

From HW

$$b. \textcircled{1} \quad 3x - 2y + 5z = -17$$

$$\textcircled{2} \quad 2x + 4y - 3z = 29$$

$$\textcircled{3} \quad 5x - 6y - 7z = 7$$

Combine $\textcircled{1} + \textcircled{2}$ to eliminate y :

$$\begin{array}{r} 2(3x - 2y + 5z = -17) \Rightarrow 6x - 4y + 10z = -34 \\ 2x + 4y - 3z = 29 \Rightarrow + (2x + 4y - 3z = 29) \\ \hline \end{array}$$

$$\textcircled{4} \quad 8x + 7z = -5$$

Combine $\textcircled{1} + \textcircled{3}$ to eliminate y :

$$\begin{array}{r} -3(3x - 2y + 5z = -17) \Rightarrow -9x + 6y - 15z = 51 \\ 5x - 6y - 7z = 7 \Rightarrow + (5x - 6y - 7z = 7) \\ \hline \end{array}$$

$$\textcircled{5} \quad -4x - 22z = 58$$

Now solve the system of $\textcircled{4}$ and $\textcircled{5}$:

$$\textcircled{4} \quad 8x + 7z = -5 \Rightarrow 8x + 7z = -5$$

$$\textcircled{5} \quad 2(-4x - 22z = 58) \Rightarrow + (-8x - 44z = 116)$$

$$-37z = 111$$

$$\boxed{z = -3}$$

Sub $z = -3$ into $\textcircled{4}$

$$8x + 7z = -5$$

$$8x + 7(-3) = -5$$

$$8x - 21 = -5$$

$$8x = 16$$

$$\boxed{x = 2}$$

Sub $x = 2, z = -3$ into $\textcircled{3}$

$$5x - 6y - 7z = 7$$

$$5(2) - 6y - 7(-3) = 7$$

$$10 - 6y + 21 = 7$$

$$-6y + 31 = 7$$

$$-6y = -24$$

$$\boxed{y = 4}$$

$$\begin{array}{l} x = 2 \\ y = 4 \\ z = -3 \end{array}$$

Applications of Systems of Equations (3x3)

The Natural Remedy Company makes 3 different essential oil blends:

Blend A: 2ml of peppermint oil; 3ml of geranium oil (5ml)

Blend B: 4ml of geranium oil; 1ml of citrus oil (5ml)

Blend C: 3ml of peppermint oil; 2ml of citrus oil (5ml)

The company has received a supply of 38 ml of peppermint oil; 110ml of geranium oil and 32 ml of citrus oil.

How many 5ml bottles of each blend can they make in order to use up all the supplies?

① Define your variables:

let A be the number of bottles of blend A

B be the number of bottles of blend B

C be the number of bottles of blend C

② Organize info in a table / make up equations:

	Peppermint	Geranium	Citrus
Blend A	2ml	3ml	0
Blend B	0	4ml	1ml
Blend C	3ml	0	2ml
TOTAL	38ml	110ml	32ml

Peppermint: ① $2A + 0B + 3C = 38$

Geranium: ② $3A + 4B + 0C = 110$

Citrus: ③ $0A + 1B + 2C = 32$

Eliminate A from ① and ②

$$\begin{array}{r} 3(2A + 3C = 38) \Rightarrow 6A + 9C = 114 \\ -2(3A + 4B = 110) \Rightarrow -6A - 8B = -220 \\ \hline \textcircled{4} 9C - 8B = -106 \end{array}$$

Solve the system of ③ and ④

$$\textcircled{4} -8B + 9C = -106 \Rightarrow -8B + 9C = -106$$

$$\textcircled{3} 8(B + 2C = 32) \Rightarrow 8B + 16C = 256$$

$$\begin{array}{l} \text{Sub } C=6 \text{ into } \textcircled{3}: \\ B + 2C = 32 \\ B + 2(6) = 32 \\ B + 12 = 32 \\ \underline{B = 20} \end{array}$$

$$\begin{array}{l} \text{Sub } C=6, B=20 \text{ into } \textcircled{1} \\ 2A + 3C = 38 \\ 2A + 3(6) = 38 \\ 2A + 18 = 38 \\ 2A = 20 \\ \underline{A = 10} \end{array}$$

25C = 150
C = 6
6 bottles of C
10 bottles of A
20 bottles of B

TO DO

- ① Group Work - Applications of 3×3
- ② p34|38+39 (OLD - from last class)
- ③ p38|6, p42|15, 19a+c (NEW! Do for HW)